

## 代数 2 H 班 作业 14

2023 年 8 月 2 日

We always denote by  $R$  a commutative ring.

**题 1.** *Let  $R[x]$  be a Jacobson ring. Prove that  $R$  is a Jacobson ring. In the previous exercises, you proved that the Jacobson radical of  $R[x]$  is equal to its nilradical. So taking  $R$  a non-Jacobson ring, you obtain an example  $R[x]$  whose Jacobson radical is equal to its nilradical but not Jacobson.*

**题 2.** *Let  $R$  be a ring. Let  $X_0 = \text{Spec}_m R$  be the subset of  $X = \text{Spec } R$  consisting of all the closed points of  $X$ . Prove that  $R$  is Jacobson if and only if for all closed subset  $Z$  of  $X$ , we have  $Z \cap X_0$  being dense in  $Z$ .*